

THREE-BLADED HORIZONTAL AXIS WATER TURBINE SIMULATIONS WITH FREE SURFACE EFFECTS

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The water level above a hydrokinetic turbine is likely to vary throughout the season and even along the day. In this work, the influence of the free surface on the performance of a three bladed horizontal-axis turbine is explored by means of a three-dimensional, transient, two-phase flow computational model implemented in the commercial CFD software ANSYS Fluent 19.0. The $k - \omega$ SST Transition turbulence model coupled with the Volume of Fluid (VOF) method is used to track the air-water interface. The rotor diameter is $D = 0.8m$. Two operating conditions are analyzed: deep tip immersion ($0.55D$) and shallow tip immersion ($0.19D$). Three tip speed ratios are evaluated for each immersion. Simulation results show a good agreement with experimental data reported in the literature, although the computed torque and thrust coefficients are slightly underestimated. Details of the free surface dynamics, the flow past the turbine and the wake near the rotor are also discussed.

Key words: Hydrokinetic turbine, VOF, sliding mesh, torque coefficient.

1. Introduction

Hydrokinetic energy is currently an active field of research, considering its potential to provide electricity to rural communities settled next to a river in developing countries (Laín, [1]; Ishak, [2]). Hydrokinetic turbines have been mostly applied to small scale generation while marine applications focus on large scale output (Muratoglu and Yuce, [3]). The main advantage of hydrokinetic technology is the possibility of obtaining energy without the need of large reservoirs, making no emissions and a minimal environmental impact. Horizontal-axis water turbines are self-starting machines and they are less prone to shaking and vibration, contrary to vertical-axis water turbines (Kirke and Lazauskas, [4]). For this reason, this study focuses on the performance of a horizontal-axis water turbine. To understand the flow dynamics and improve the turbine efficiency, computational and experimental approaches have been explored in recent years (Bahaj, [5]; Yan, [6]; Bahaj, [7]; Contreras, [8]). In that sense, Computational Fluid Dynamics (CFD) is an essential approach to analyze the fluid flow through the turbine rotor and to estimate its performance. Some numerical techniques such as blade-element-momentum (BEM) methods have been successfully employed (Batten *et al.*, [9, 10]). Batten *et al.*, [9] explored and validated a BEM implementation with the use of their experimental results in a cavitation tunnel and a towing tank. In a similar way, Danao *et al.*, [11] reported turbine performance calculations with the open source blade element - momentum solver QBlade, showing acceptability and appropriateness of the model. However, BEM cannot be employed if the turbine interacts with the free surface or if the structure that holds the turbine rotor needs to be considered. Also, the wake that

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develops downstream cannot be resolved with BEM. On the other hand, three-dimensional, transient fluid flow computations provide an accurate representation of the wake downstream the rotor (Abuan and Howell, [12]).

The water level above hydrokinetic turbines can change throughout the season and even along the day. Considering the operation of a turbine in low flow and shallow rivers, the distance to the free surface can change continually in such a way as to affect the turbine overall performance. Previous numerical works have mostly ignored the effects of rotor depth, which could be very important specially for shallow-tip immersions. The main reason is the computational cost for solving two-phase flow equations. However, free-surface effects can greatly affect the overall performance so they have been considered on previous investigations (Bai, [13]; Yan, [6]; Benchikh [14], Nishi [15]). Benchikh *et al.*, [14] investigated a Darrieus vertical axis hydrokinetic turbine under the presence of a free surface using the volume of fluid (VOF) method and the unsteady $k - \omega$ SST turbulence model. Their two-phase flow simulation results showed little discrepancy with experimental data of Koshizuka *et al.*, [16]. Their results also showed that single-phase flow computations (in the absence of a free surface) overestimate the power coefficient. Bai *et al.*, [13] used an immersed boundary method and a free surface method with extensive validation cases including the water turbine of Bahaj *et al.*, [5]. The reported discrepancy between simulation results and measurements of the power coefficient were about 4% for deep tip immersion. Yan *et al.*, [6] presented a computational free-surface flow framework and a novel level-set re-distancing procedure with an excellent agreement related to experimental results. In general, simulation results show a reduction in the power coefficient when the rotor is close to the free surface, which agrees well with experimental observation, except for the results reported by Nishi *et al.*, [15]. Also, a power enhancement zone has been reported which suggests an optimal distance from the free surface (Kolekar *et al.*, [17]). It is expected from previous works that single-phase flow simulations predict a similar performance to deep tip immersion configurations.

The hydrodynamic performance of a three-blade horizontal axis hydrokinetic turbine is studied in this work by means of numerical simulations. The computational model considers free surface effects, i.e. the air-water interface. The turbine geometry is taken from the literature [5] which also reports experimental data. Two immersions: deep tip immersion ($0.55D$) and shallow tip immersion ($0.19D$) were simulated, each one at three tip speed ratios (TSR): 4, 6 and 8. This work deals with transient simulations incorporating a Transition Shear Stress Turbulence Model. To the best of authors knowledge, it is the first time such a turbulence model, coupled with VOF, is used in numerical simulations of hydrokinetic turbines. A quantitative description of the free surface displacement and the asymmetry of the rotor wake are the main contributions of this work to the current state of the art on the simulation of horizontal axis river turbines.

This paper is organized as follows: In section 2, the turbine layout, the computational domain and its discretization are described. Section 3 provides a detailed description of the computational model. The computed performance coefficients and the discussion of results is found in section 4. Finally, the last section presents the conclusions and future work.

2. Geometry and discretization

The rotor diameter of the simulated hydrokinetic turbine is $D = 0.8\text{ m}$. The blades are based on the profile shape of a NACA 63-8XX, and the information about the chord, thickness and pitch was taken from [5]. The computational domain consists of two sub-domains: a rotating part and a steady one. The rotating domain has the shape of a cylinder and includes the turbine rotor. 86% of the cells in the computational domain are found in the rotating cylinder; mesh refinement is necessary along the rotor blades in order to fulfill the near wall treatment. Fifteen layers with an inflation of 1.2 were set in ANSYS Meshing 19.0 to mesh the blades and hub walls. The static domain is prismatic with an inner hole to fit the rotating domain. Different mesh sizes were employed in order to improve the resolution of the domain interfaces, the downstream wake and the free surface interface. To ensure mesh quality, skewness was checked to be less than 0.78 all over the domain with an average value of 0.28 in all meshes used.

The size of the computational domain is parameterized in terms of the rotor diameter, D : length $10D$, height and width $3.5D$, with the rotating sub-domain located at $3D$ from the domain inlet, as it is shown in Fig. 1.

The blockage ratio, defined as the ratio of rotor swept area to the channel cross-sectional area (Daskiran *et al.* [18]), is 6.4 % when the domain is filled up with water, 8.01% for deep tip immersion (0.55D) and 9.2% for shallow tip immersion (0.19D). In spite of having quite high blockage ratios, it has been reported that blockage ratios below 10%, do not significantly affect the turbine performance, thus no blockage corrections are considered (Kolekar *et al.*, [19]).

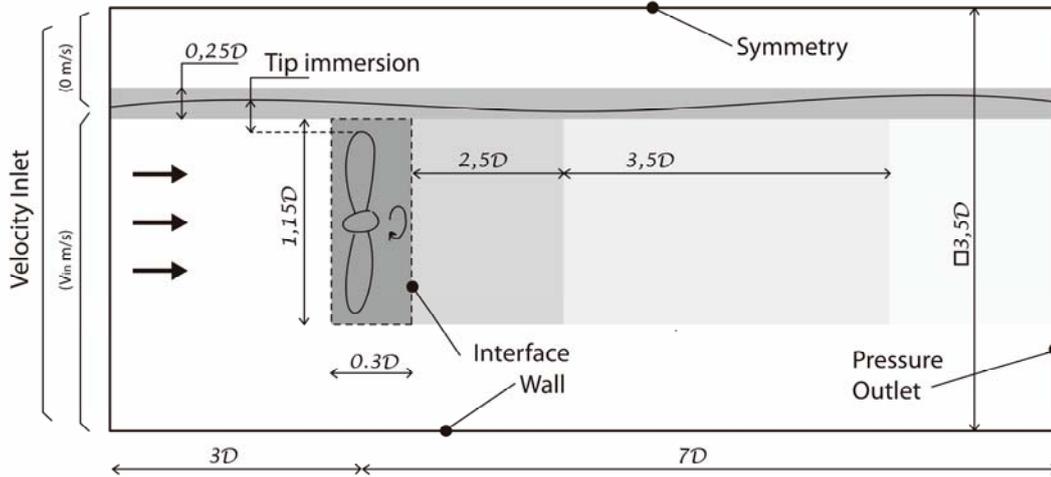


Fig.1. Schematic of the computational domain and boundary conditions. The domain height and width is 3.5D. Dark areas highlight mesh refinement zones.

3. Computational approach

Transient simulations were computed in ANSYS 19.0. In order to simulate the rotor rotation, one portion of the domain rotates at a constant angular velocity by means of a sliding mesh technique. In that approach, the cylindrical sub-domain that contains the rotor and hub rotates while the interface between rotating and static sub-domains is updated at every time step. The volume of fluid (VOF) method was used to track the air-water interface. VOF computes the volume fraction of one phase (i.e. water) to follow the free surface deformation (Koshizuka, [16]; Benchikh, [14]) The solved transport equations are: equation of mass, equation of momentum and equation of volume conservation, respectively (Nishi *et al.*, [15])

$$\frac{\partial}{\partial t}(\alpha_W \rho_W) + \frac{\partial}{\partial x_j}(\alpha_W \rho_W v_j) = 0, \tag{3.1}$$

$$\frac{\partial}{\partial t}(\rho v_i) + \frac{\partial}{\partial x_j}(\rho v_i v_j) = \frac{\partial P}{\partial x_i} + \frac{\partial}{\partial x_j} \left[\mu \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) - \overline{\rho v_i v_j} \right] + f_i + \rho g_i, \tag{3.2}$$

$$\alpha_W + \alpha_A = 1 \tag{3.3}$$

where subscripts *W* and *A* refer to water and air phases, respectively; *i* and *j* are indices, *f* is the external body force per unit volume. The Reynolds stresses $\overline{\rho v_i v_j}$ are computed according to the turbulence models described below. Furthermore, the viscosity μ and the fluid density ρ are given by,

$$\mu = \alpha_W \mu_W + \alpha_A \mu_A, \quad (3.4)$$

$$\rho = \alpha_W \rho_W + \alpha_A \rho_A. \quad (3.5)$$

The RANS $k - \omega$ Shear Stress Transport (SST) turbulence model (Menter, [20]) was initially used for the computations. In order to better resolve the flow, the four-equation transition SST model (Langtry and Menter, [21]) was implemented. Most of the single-phase simulations and all of the two-phase flow computations were performed with the transition turbulence model. This approach is known to improve the accuracy of turbine performance computations compared to two-equation eddy viscosity turbulence models (Rezaeiha *et al.*, [22]).

The free surface reconstruction is based on the modified HRIC (High Resolution Interface Capturing scheme). It has reported good quantitative and qualitative agreement in spite of artificial effects and diffusivity (Waclawczyk and Koronowicz, [23]). Pressure-velocity coupling is achieved by the SIMPLE approach and second order upwind schemes are specified for the numerical solution. A uniform velocity of 1.5 m/s is set at the inlet boundary for water (Bahaj *et al.*, [5]). Air velocity was set to zero at inlet and in the air zone above the free surface, see Fig.1. Temporal discretization was chosen such that a blade rotates less than one degree per time-step, which leads to the data presented in Tab.1. for each TSR.

Table 1. Minimum and maximum time steps (Δt) used in the two-phase flow computations.

TSR	Δt_{min} (s)	Δt_{max} (s)
4	5×10^{-4}	1×10^{-3}
6	1×10^{-4}	7.5×10^{-4}
8	1×10^{-4}	5×10^{-4}

A maximum of 50 iterations per time-step was set in order to lower the residuals and satisfy the convergence criterion of 1×10^{-6} , except for the specific turbulence frequency, ω , whose residual reached 1×10^{-4} . Single-phase flow computations with the $k - \omega$ SST turbulence model and a multiple reference frame (MRF) were first performed to initialize the computational solution. This preliminary solution was used as an initial guess in the two-phase flow computations. The air zone was patched to zero velocity and zero water volume fraction. First order schemes were used a few time steps before switching to second order schemes. The computations were run for nine seconds which leads to 21.5, 32.2 and 43.0 blade rotations for TSR 4, 6 and 8, respectively. The non-dimensional parameters that describe the performance of horizontal axis turbines are the tip speed ratio (TSR), the power (C_p) and thrust (C_T) coefficients. TSR relates angular velocity to the incoming fluid velocity:

$$TSR = \frac{\Omega D}{2V_{in}} \quad (3.6)$$

where Ω is the rotor angular velocity, D is the diameter, and V_{in} is the incoming water velocity. Simulation results presented in this work were obtained for three tip speed ratios (TSR): 4, 6 and 8. Power coefficient (C_p) and torque coefficient (C_m) are defined by,

$$C_p = \frac{W}{\frac{1}{2} \rho V_{in}^3 A}, \quad C_m = \frac{C_p}{TSR} \quad (3.7)$$

where ρ is the fluid density (water in this case), A is the area swept by the rotor ($\pi D^2 / 4$) and W is the power produced by the turbine. The thrust coefficient is related to normal force acting on the rotor, F_T , and is expressed as,

$$C_T = \frac{F_T}{\frac{1}{2} \rho V_{in}^2 A}. \quad (3.8)$$

The estimated values of C_m and C_T by CFD are compared with experimental data taken from the literature [5].

4. Results

Before performing two-phase flow computations, single phase (water) simulations were run with two different turbulence models: the two equation SST $k - \omega$ model and the four-equation transition SST model. The torque coefficient calculated with the SST $k - \omega$ and four-equation transition turbulence models at $TSR=6$ is presented in Fig.2. These are single-phase flow results. As part of the grid independence study, three simulations were performed with the SST transition model and four additional simulations with the two-equation SST model. Data points are connected by interpolation functions in Fig.2. As it can be observed, a higher C_m is obtained when the four-equation SST transition turbulence model is used. The computed C_m is slightly underestimated when it is compared to the experimental result reported by Bahaj *et al.*, [5]. A better agreement is achieved with the four-equation turbulence model due to its ability to account for the laminar-to-turbulent transition on the blade surface ([Marsh, [24]; López, [25]; Langtry, [21]). On the other hand, the transition model increases the computational cost by about 30% [24]. Figure 2 also shows that the difference between calculations of C_m with the turbulence models is about 5% for a 8.5 million cell mesh and larger meshes. In order to improve the calculations of C_m and C_T , the transition turbulence model is used in all two-phase flow simulations with a mesh of 7.1 million cells.

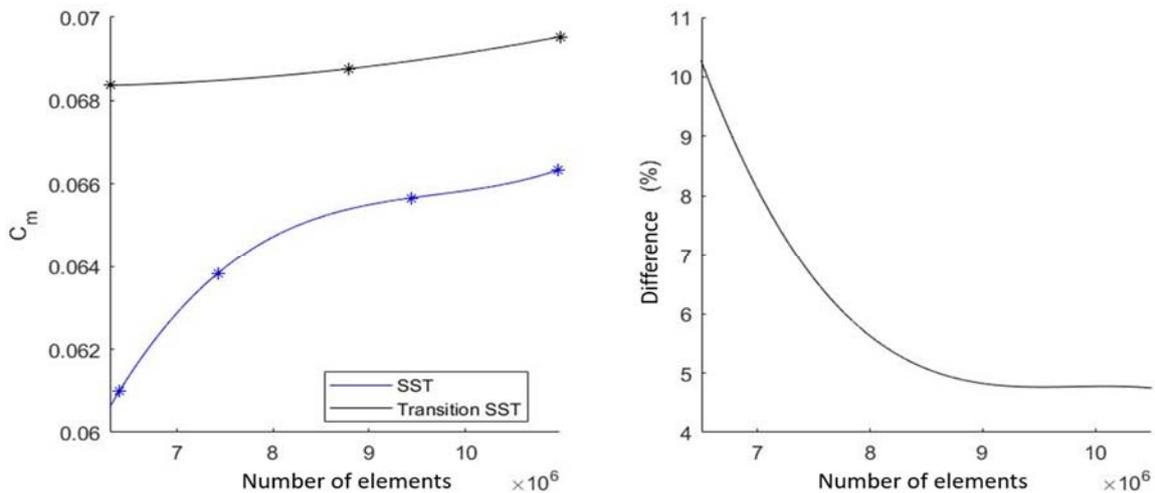


Fig.2. Sensitivity to turbulence model. Prediction of torque coefficient (left). Percentage difference between the turbulence models (right). $TSR=6$.

Figure 3 compares the computed C_m and C_T with the experimental data of Bahaj *et al.* [5] and for two rotor depths, namely deep tip immersion ($0.55D$) and shallow tip immersion ($0.19D$). In addition, MRF

steady-state results, which correspond to single-phase computations are also included. In general, there is a good qualitative agreement between numerical and experimental data for the three analyzed TSRs; it can be observed that the computed C_m and C_T follow the same trend as the experiments. The torque coefficient rises a little as the rotor depth increases. The percentage difference between numerical results and experimental data goes from 13% to 22% for C_m , and 12% to 20% for C_T . The lowest discrepancy in C_m is obtained for $TSR=6$, while for C_T the discrepancy grows with TSR . Compared with the stationary result (MRF), a lower torque coefficient is obtained when transient calculations are performed. MRF simulations show a slightly lower thrust coefficient, although the C_T trend looks quite similar to the transient simulation results. The numerical results show lower torque and thrust coefficients when the turbine runs close to the free surface, which agrees well with experimental observations. The highest power coefficient is obtained at $TSR=6$, i.e. the design point.

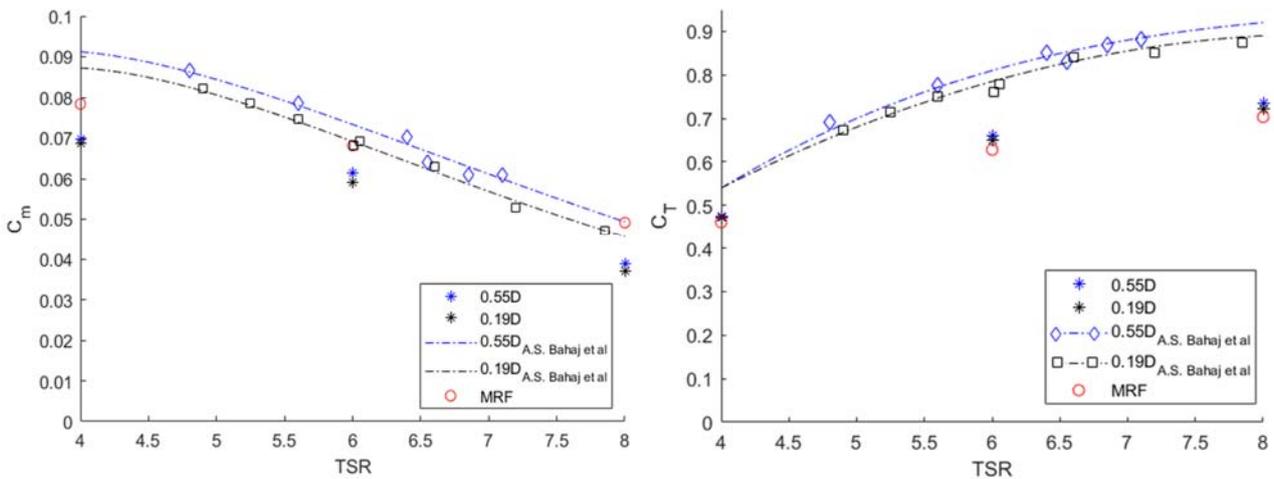


Fig.3. Time-average results of torque and thrust coefficients for three tip speed ratios and at two rotor depths. Circles represent steady-state MRF results (single-phase).

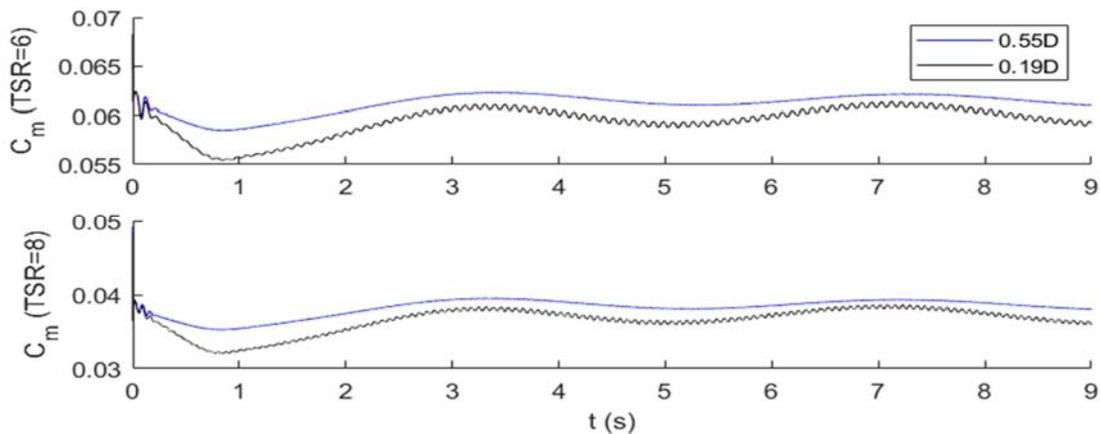


Fig.4. Transient behavior of torque coefficient at two rotor depths.

Time-average values of C_m are obtained from transient, two-phase flow simulations. The time series is recorded over a 9s period, as it can be observed in Fig.4. TSRs of 6 and 8 which correspond to 32.2 and 43.0 blade rotations, respectively. It can be noticed that high frequency oscillations are superimposed to the

sinusoidal response of the rotor for the shallow tip immersion ($0.19D$). This distinctive behavior can be attributed to the proximity of the free surface. The large period of the sinusoidal wave is approximately the same for both tip immersions and TSRs. The wave amplitude is slightly higher in the case of $0.19D$ immersion. The high frequency oscillations are related to the rotor angular velocity, and therefore the TSR. That frequency is exactly three times the rotation rate of the three-bladed rotor. The low frequency oscillation of C_m is independent of the rotor angular velocity and it is approximately the same for all the hub immersions and all the tip speed ratios simulated.

Figure 5 illustrates the variation of C_m over one revolution, and Fig.6. shows the contribution of each blade. As it is clearly seen, the contribution of each blade to the torque coefficient combines to produce a fairly constant output for deep immersion and a roughly sinusoidal response for shallow immersion. The alternation in both, torque and thrust, decreases when increasing the immersion. When the blade tip is at the deepest position the contribution of that blade to C_m is the highest. This feature is emphasized at shallow immersions. The alternation in torque also implies alternation in loads that could induce blade fatigue in the long run, especially for shallow tip immersions. It is important to realize that the behavior is not strictly sinusoidal as it is changing in time as observed in Fig.4. Results from single-phase flow simulations do not exhibit this variation.

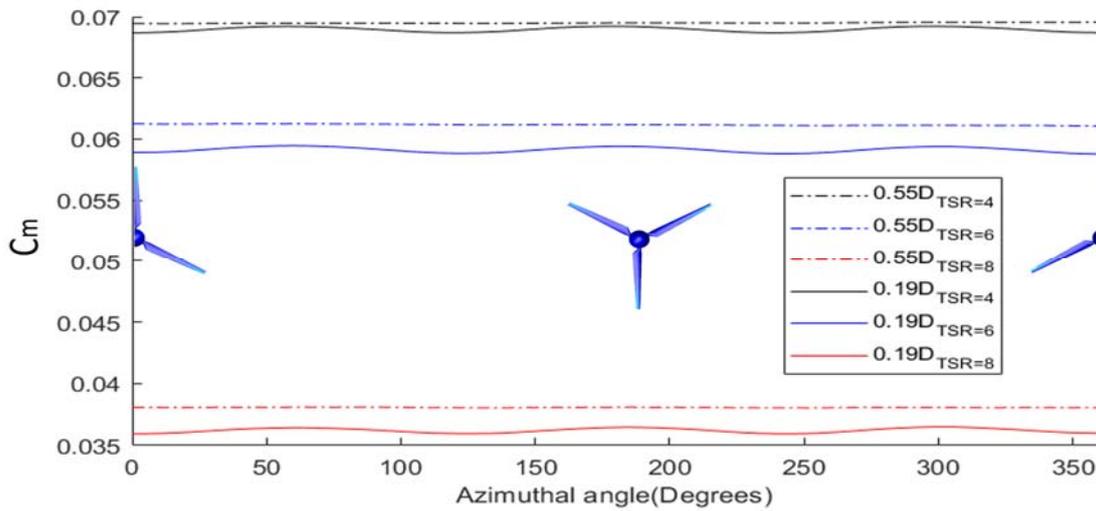


Fig.5. C_m variation over one revolution at various TSRs and rotor depths.

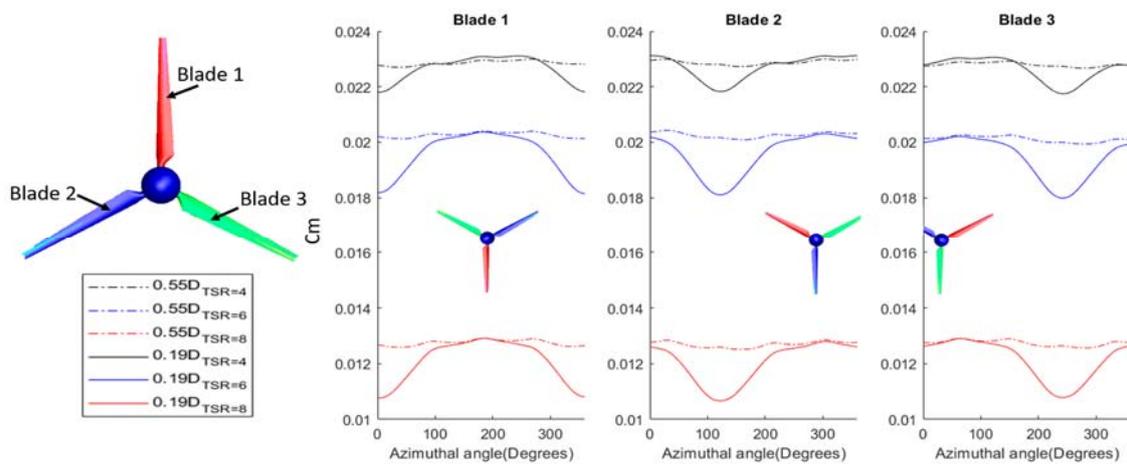


Fig.6. Blade contribution to the torque coefficient over one revolution.

The vertical displacement of the free surface, normalized by the rotor diameter, at the domain mid-plane is shown in Fig.7. The displacement is obtained at the design tip speed ratio, $TSR=6$, and it is compared at the two rotor depths. Simulation results confirm a larger deformation just upstream and downstream the rotor for the shallow tip immersion. As the flow approaches the rotor the water slows down and its kinetic energy is modified. Some of the fluid must be diverted in order to satisfy mass conservation and the free surface must rise directly upstream of the rotor. The effect is more noticeable when the tip distance to free surface is decreased. Also, the waves formed immediately behind the rotor rapidly dissipate as the water flows downstream. The result presented in Fig.7. demonstrates the correct tracking of the free surface. It is important to mention that the height of the air-water interface is prescribed by the inlet boundary condition. Therefore, the interface may not be properly calculated in the vicinity of the inlet boundary. The free surface deformation is likely to be accentuated if the main body and upright of the turbine are included in the computational model (Myers and Bahaj, [26]).

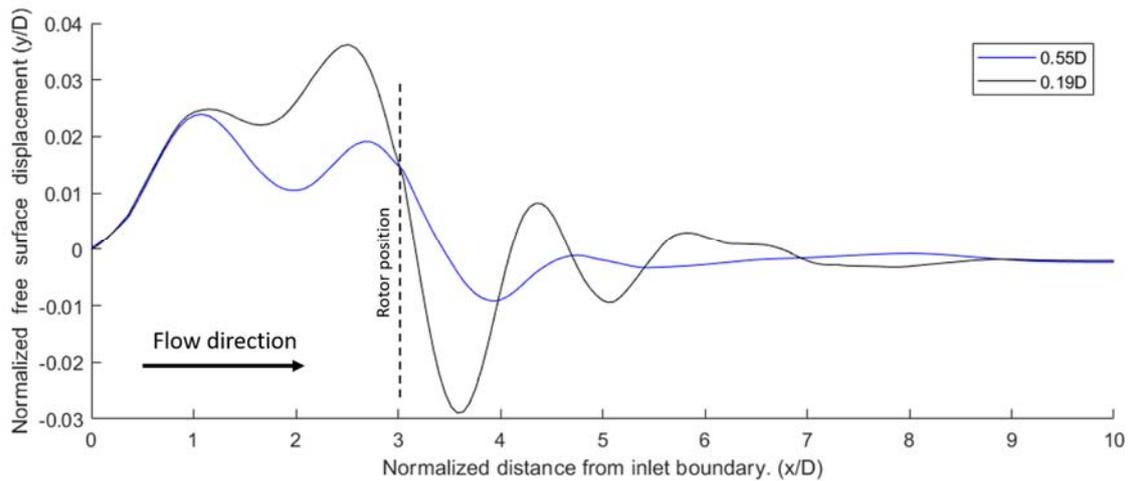


Fig.7. Vertical displacement of the free surface at the channel mid plane. Results for $TSR=6$ and two rotor depths (time $9s$).

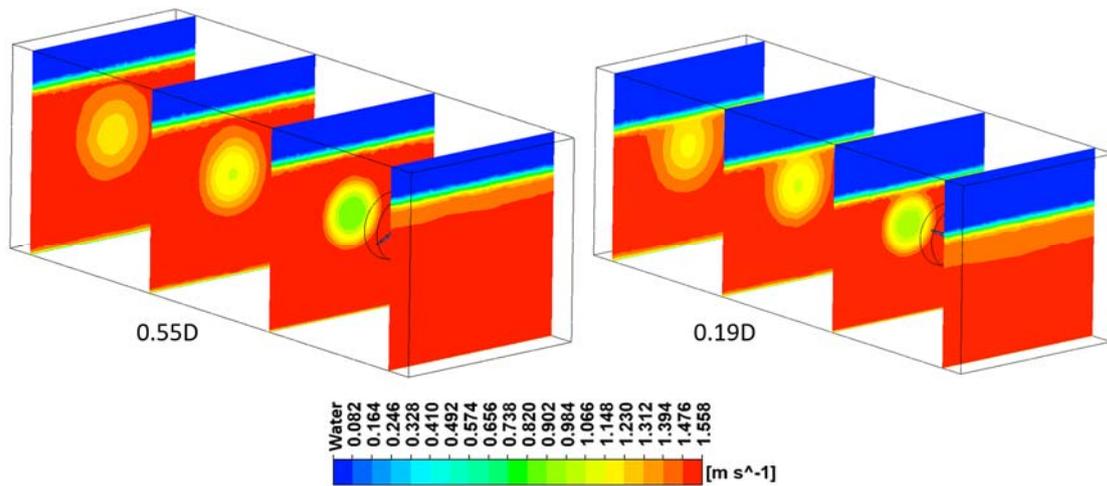


Fig.8. Axial velocity contours for rotor depths $0.55D$ and $0.19D$ ($TSR=6$).

Axial velocities in four planes ($1D$, $4D$ and $6.5D$ downstream and $1D$ from entrance) are shown in Fig.8. for the two analyzed tip immersions at $TSR=6$. The velocity deficit is clearly observed downstream. Also, non-

symmetrical axial velocity profiles are observed when the rotor is closer to the free surface. Previous works (Adamski, [27]) have reported asymmetrical wakes for hub immersions lower than $1.5D$, which agrees well with the results presented here. The minimum axial velocity in the wake is found off the rotor centerline and towards the free surface, contrary to single-phase flow simulations that show a symmetric wake with a minimum velocity exactly at the centerline.

5. Conclusions

Two-phase flow simulations of a three-bladed horizontal axis hydrokinetic turbine are presented in this paper. The computational approach includes a transition turbulence model, the VOF method for interface tracking and the sliding mesh technique to account for blade rotation. Simulation results are evaluated at three different TSR resulting in an acceptable agreement with experimental observations. The implementation of the Transition SST four-equation turbulence model leads to higher values for the torque coefficient. The time dependent behavior of C_m shows high frequency oscillations when the rotor is close to the free surface ($0.19D$). It suggests that hydrokinetic turbines operating in shallow rivers are likely to be exposed to cyclic blade loads. A higher displacement of the free surface is also observed for the shallow tip immersion, and it occurs in the vicinity of the rotor. A non-symmetrical wake is observed for the shallow tip immersion which reflects the interaction between the wake and free surface.

Future work will focus on incorporating the turbine main body and upright in the computational model. The domain size and mesh quality will be further assessed. The distance from the inlet boundary to the rotor subdomain will be varied to study the effect on the free surface. Similar computations for other tip immersions will also be necessary to properly characterize the turbine performance.

Nomenclature

A	– area swept by the rotor
C_m	– torque coefficient
C_p	– power coefficient
C_T	– thrust coefficient
D	– diameter
f_i	– external body force per unit volume
F_T	– normal force acting on the rotor
Δt	– time steps
TSR	– tip speed ratio
v_i	– fluid velocity in i direction
V_{in}	– incoming water velocity
W	– power produced by the turbine
α_A	– air volume fraction
α_W	– water volume fraction
μ_A	– air Dynamic viscosity
μ_W	– water Dynamic viscosity
ρ_A	– air density
ρ_W	– water density
Ω	– angular velocity

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